

***Probability of Detection Tutorial Workshop Sessions***

***1993 ASNT Spring Conference  
March 29-April 2***

***Speaker Hand-Outs***



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**Probability of Detection  
Tutorial Workshop Sessions**

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Presented in Nashville on Wednesday, March 31

**Chairmen:**

**Derek Sturges, GE Aircraft Engines  
Cincinnati, OH**

&

**Steve Cargill, Pratt & Whitney  
W. Palm Beach, FL**

Table of Contents:

<b>Historical Overview of Approaches to POD</b>	<b>1</b>
D. Sturges, GE Aircraft Engines	
<b>Elements of Detection Theory Applied to NDE</b>	<b>41</b>
D. Sturges, GE Aircraft Engines	
<b>Quantifying Non-Destructive Evaluation Capability and Reliability</b>	<b>74</b>
C. Annis, United Technologies	
<b>The Relative Operating Characteristic Approach to Probabilities of Detection and False Alarm</b>	<b>109</b>
D. Sturges, GE Aircraft Engines	
<b>The Role of Physical Modeling of Inspection Processes:</b>	<b>152</b>
B. Thompson, Iowa State University	

**HISTORICAL OVERVIEW OF APPROACHES TO POD**

**Derek Sturges  
GE Aircraft Engines  
Engine Support Operation  
Cincinnati, Ohio**

**Tutorial Workshop on Probability of Detection  
Spring 1993 ASNT Conference**

**THINK OF AN NDE PROCESS WITH WHICH YOU ARE FAMILIAR**

**o WHAT SIZE DEFECTS IS IT CAPABLE OF DETECTING?**

**- HOW DO YOU KNOW THAT?**

**o WHAT PROPORTION OF THOSE DEFECTS ARE DETECTED?**

**- HOW DO YOU KNOW THAT?**

**o TODAY'S PROGRAM WILL HELP ANSWER THOSE QUESTIONS!**

**THINK OF TWO NDE PROCESSES**

o WHICH PROCESS FINDS THE SMALLEST DEFECTS?

- HOW DO YOU KNOW THAT?

o WHICH PROCESS FINDS THE MOST DEFECTS?

- HOW DO YOU KNOW THAT?

o TODAY'S PROGRAM WILL HELP ANSWER THOSE QUESTIONS!

**THINK OF TWO NDE INSPECTORS YOU KNOW**

o **DO THEY BOTH PERFORM EQUALLY WELL?**

- **HOW DO YOU KNOW THAT?**

o **DOES THEIR PERFORMANCE MEET YOUR NEEDS?**

- **HOW DO YOU KNOW THAT?**

o **TODAY'S PROGRAM WILL HELP ANSWER THOSE QUESTIONS!**

**YOUR COMPANY MAKES CYCLICALLY-LOADED PRODUCTS**

o **HOW MUCH WILL BETTER INSPECTION IMPROVE PRODUCT LIFE?**

- **HOW DO YOU KNOW THAT?**

o **WHEN SHOULD YOU SCHEDULE AN IN-SERVICE INSPECTION?**

- **HOW DO YOU KNOW THAT?**

o **TODAY'S PROGRAM WILL HELP ANSWER THOSE QUESTIONS!**

## **OUTLINE OF THE TUTORIAL WORKSHOP ON POD**

- o **HISTORICAL OVERVIEW OF APPROACHES TO POD (Sturges)**
  - Some basic concepts of capability and reliability
  - An outline of techniques for measuring capability
  
- o **ELEMENTS OF DETECTION THEORY (Sturges)**
  - Defining "detection"
  - Detection in a signal-to-noise context
  
- o **ELEMENTARY STATISTICAL CONCEPTS FOR POD ANALYSIS (Annis)**
  - Probability distributions and related topics
  - Sampling concepts and prediction intervals
  
- o **THE ROC APPROACH TO POD AND PFA (Sturges)**
  - An outline of statistical detection concepts
  - Radar origins, and applications to NDE



## **OUTLINE OF THE TUTORIAL WORKSHOP ON POD**

- o **US AIR FORCE APPROACHES TO POD (Annis)**
  - Methods for data acquisition and analysis
  - Advantages and limitations
  - Aerospace applications
  
- o **ROLE OF PHYSICAL MODELLING OF NDE PROCESSES (Thompson)**
  - Modelling the contribution of individual inspection parameters
  - Examples of POD analyses
  
- o **SELECTING AND APPLYING POD METHODS (panel)**
  - Charles Annis                   United Technologies
  - Michael Avioli                Electric Power Research Institute
  - Charles Salkowski          National Aeronautics and Space Administration
  - Derek Sturges                General Electric Aircraft Engines
  - Bruce Thompson            Center for NDE, Iowa State University
  - Sharon Vukelich            US Air Force

## **CONCEPTS OF CAPABILITY AND RELIABILITY**

### **o DICTIONARY DEFINITIONS**

- CAPABLE: "having capacity or ability; able to do things well; skilled; competent; efficient; able"**
- RELIABLE: "can be relied on; dependable; trustworthy"**

### **o INDUSTRIAL QUALITY DEFINITION (Juran & Gryna, Quality Planning & Analysis)**

- RELIABILITY: "the probability of a product performing without failure a specified function under given conditions for a specified period of time"**

### **o NDE DEFINITION (Packman et al., Metals Handbook, 8th edition)**

- RELIABILITY: "A quantitative measure of the efficiency of (an NDE) procedure in finding flaws of a specific type and size"**

## **CONCEPTS OF CAPABILITY AND RELIABILITY**

### **o CAPABILITY OR RELIABILITY?**

- Different concepts - but often used interchangeably!
- Packman's definition works for both

### **o NDE SYSTEM CAPABILITY/RELIABILITY**

- Inspection processes involve numerous factors
- Variations in instrumentation, inspector performance, etc.
- Do these affect Capability and Reliability equally?

### **o THERE IS NEED FOR A TERMINOLOGY STANDARD**

## SUGGESTED DISTINCTIONS IN TERMINOLOGY

- o **RELIABILITY:** (Haines, Sturges, Abernethy, Thompson)
  - Composite effect of the following sources of variation
  - **CAPABILITY:** Defect detectability determined by physics
    - Detection of defects of the same nominal size
  - **REPEATABILITY:** Changes in performance with time
    - Reinspection by the same inspector or inspection system
  - **REPRODUCIBILITY:** Differences in nominally identical systems
    - Reinspection after process changes
  - **VARIABILITY:** Effects of human factors
    - Reinspection by another inspector or inspection system
- o **RELIABILITY:** (Avioli)
  - The probability that no flaw exists, given that the inspection process indicates that there is no flaw; (the probability of correct acceptance)

**CAPABILITY FROM CALIBRATION**

**o TRUE STATEMENT**

- Ultrasonic inspection can reject all indications larger than that from a  
0.0008 sq. in. planar void

**o THE SUPPORTING EVIDENCE**

- Inspection is calibrated from a 3/64" diameter flat-bottomed hole (FBH);  
indications above 50% of that reference level are rejected

**o THE PROBLEM**

- No measure of what size defect would be detected or rejected
- Might be misinterpreted as stating all 0.0008 defects rejected

## **CAPABILITY FROM PRECEDENT**

### **o TRUE STATEMENTS**

- 1 mm long cracks can be detected with Fluorescent Penetrant Inspection
- FPI is capable of detecting 1 mm long cracks

### **o THE SUPPORTING EVIDENCE?**

- An indication detected by FPI was caused by a 1 mm crack

### **o THE PROBLEM**

- No measure of how many 1 mm long cracks were missed!
- Might be misinterpreted as stating all 1mm cracks detectable

**TYPICAL INDUSTRIAL UNDERSTANDING OF CAPABILITY**

- o **LIMITED TO SIMPLE STATEMENTS LIKE THE PRECEDING**
  - Correct and apparently innocuous as stated
  - Open to potentially dangerous misinterpretation
  
- o **WHAT SIZE DEFECT CAN NDE PROCESSES DETECT?**
  - Honest answer: it has usually not been established!
  
- o **HOW LONG HAVE WE HAD TO GET THE ANSWER?**
  - Major NDE processes have been used for 50 to 100 years!
  
- o **HOW DO WE EXPLAIN THIS APPARENT GAP?**
  - The question has rarely been asked!

**PROCESS CONTROL APPLICATIONS OF NDE**

**o MOST NDE APPLICATIONS IN MOST INDUSTRIES**

- **Emphasis on consistency**
- **Inspection independent of when or where conducted**
- **Calibrate from artificial defects**
- **Need reproducible reference targets for each site**

**o NDE USED IN "PACKAGE" OF PROCESS CONTROLS**

- **Typically monitor from raw material through finished product**
- **Chemical, mechanical, dimensional, etc.**
- **Success judged by favorable field-service record**



**CAPABILITY FOR REAL DEFECTS?**

**o TRUE CAPABILITY NOT ESSENTIAL FOR PROCESS CONTROL**

- Capability of individual elements in the package not needed

**o MOTIVATORS FOR MEASURING CAPABILITY**

- Quantitative comparison of various NDE processes
- Quantitative comparison of various inspectors or systems
- Need to apply NDE to management of product life

**o FACTORS LIMITING CAPABILITY MEASUREMENT?**

- Cost, and lack of agreed methodology

## **CAPABILITY FOR REAL DEFECTS?**

### **o CAPABILITY EXPRESSED IN PROBABILISTIC TERMS**

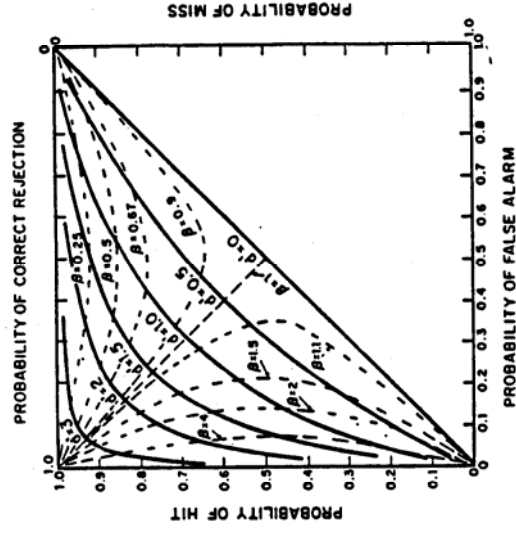
- Inspection processes are too complex to be described deterministically
- Numerous differences in defect, material, inspection process

### **o FOUR OUTCOMES TO EACH INSPECTION (each with a probability)**

- Detection of a defect that is present
- Probability of Detection (POD)
- Non-detection of a defect that is present
- Probability = (1 - POD)
- Apparent detection of a defect that is not present
- Probability of False Alarm (PFA)
- Non-detection of a defect that is not present
- Probability = (1 - PFA)

## EARLY APPROACHES TO QUANTIFYING DETECTION CAPABILITY

Family of ROC curves based on normal, equal-variance distributions (curves correspond to constant signal-to-noise and threshold)



## 0 DETECTION OF SIGNALS IN NOISE

- Statistical theory of signal detection
- Detection identified with statistical tests for validity of hypotheses
- World War II applications to communications, RADAR and SONAR
- POD and PFA derived from measurements of signal and noise
- Later combined with information theory concepts and sensory psychology
- Relative Operating Characteristic formatted by Birdsall (U. Michigan)
- Numerous applications in evaluating detection/decision processes

## **EARLY APPROACHES TO QUANTIFYING DETECTION CAPABILITY**

- o **MATHEMATICAL MODELLING OF ULTRASONICS (1950's)**
  - Theoretical description of transducer/reflector interaction
  - The flat-bottomed hole (FBH) as a defect model
  
- o **INDUSTRIAL APPLICATION BY THE KRAUTKRAMERS (and others)**
  - Krautkramer AVG/DGS diagram
  - Quantitative relation between backwall and planar disk responses
  - Defect size in terms of "Equivalent FBH" (FBH giving same indication)
  - Basis for life prediction for steam turbine & generator rotors
  - GE (1960's); ASTM Standard A418 (1974)

# THE KRAUTKRAMER DISTANCE-GAIN-SIZE DIAGRAM

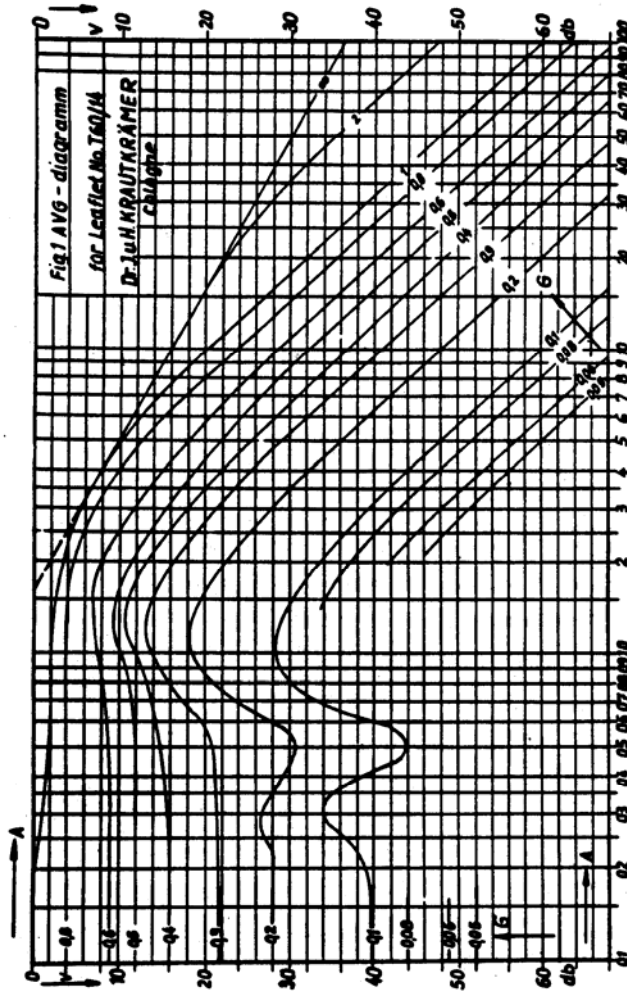


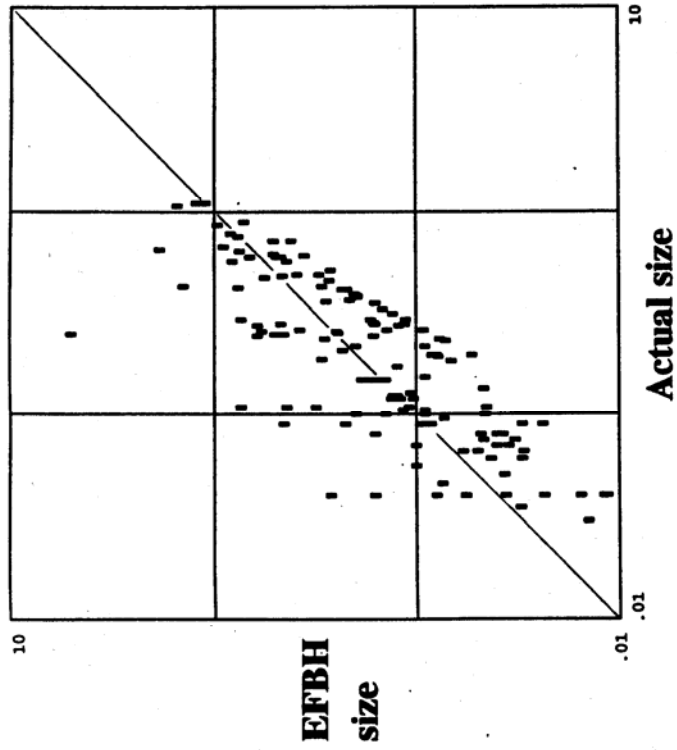
Fig 1 AVG - diagram  
for Leaflet No. T60/1A  
Dr. J. H. KRAUTKRAMER  
Chicago

A = Distance (in near-field lengths)

V = Gain (in dB)

G = Size (of a FBH relative to the transducer diameter)

## **POWER GENERATION INDUSTRY**



- o **COMPARISON OF EFBH AND ACTUAL DEFECT SIZES**
- Data used to adjust EFBH estimate for individual indications
- Modified EFBH size used in predicting rotor life

**POWER GENERATION INDUSTRY**

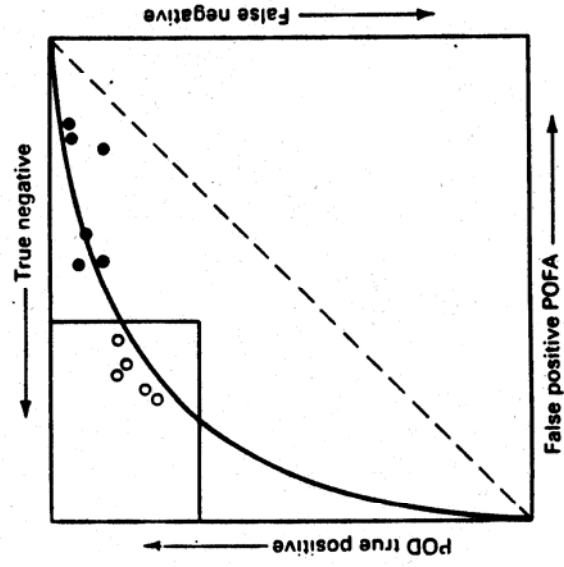
**o POD/RELIABILITY MODELLING APPROACH**

- Central Electricity Generating Board (Coffey, 1977 et seq.)
- Theoretical estimates for upper bounds on crack detection and sizing

**o RELATIVE OPERATING CHARACTERISTIC (ROC) APPROACH**

- ROC format adopted for presentation of reactor inspection data
- Used mostly to compare inspector performance
- More on this later .....

# POWER GENERATION INDUSTRY



Example of ROC presentation of data



## AEROSPACE INDUSTRY

- o **USAF, NASA, and US AEROSPACE INDUSTRY**
  - Work began in the late 1960's
  - Motivated by need for data for fracture-mechanics analysis
  - Needed to counter high cost of maintenance & replacement
  
- o **AIRFRAME INDUSTRY PROGRAMS**
  - First detailed study published in 1968
  - Fracture-control procedures initiated after loss of F-111 (1969)
  - Several major sponsored programs run in the mid-1970's
  - Lockheed-Georgia evaluated over 500,000 inspection opportunities
  - Reported POD as a function of process, material, inspector, etc.

## AEROSPACE INDUSTRY

### o PAST NASA PROGRAMS

- Awarded contracts for acquisition of quantitative NDE data (1973)
- Produced Shuttle Fracture Control Plan (1974)
  - Defect detectability based on penetrant POD data
  - Distinguished "standard" and "special" NDE capability standards
- Fracture Control applied to Shuttle main engine (1980)
- NASA FLAGRO (fracture analysis program) released (1986)

### o FUTURE NASA PROGRAMS

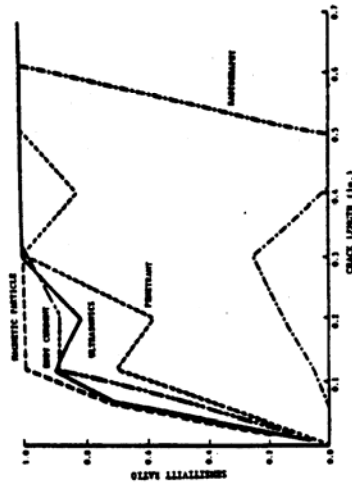
- Distribution of NASA NDE Reliability Computer Program
- Large-scale effort for fabrication of defect samples

**AEROSPACE INDUSTRY**

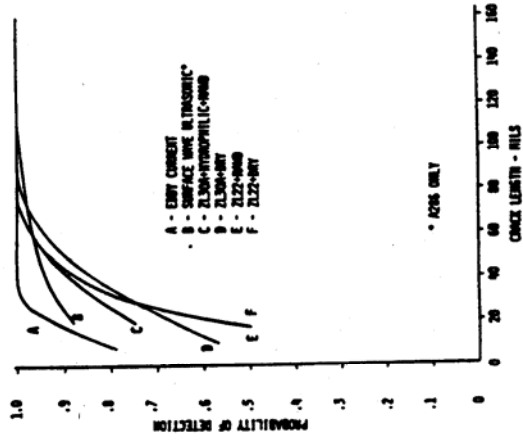
**o US AIR FORCE PROGRAMS**

- **AIRCRAFT STRUCTURAL INTEGRITY PROGRAM (ASIP)**
  - Requirements defined in MIL-STD-1530A (USAF), issued in 1975
  - First applied rigorously to B-1 bomber
  - ASIP criteria have been applied to over 20 US military planes
- **DURABILITY AND DAMAGE TOLERANCE ASSESSMENT (DADTA)**
  - Retrospective review of existing engines (initiated 1978)
- **ENGINE STRUCTURAL INTEGRITY PROGRAM (ENSIP)**
  - Requirements defined in MIL-STD-1783 (USAF), issued in 1984

# AEROSPACE INDUSTRY



Airframe data (early 1970's)



Engine data (late 1970's)

## Typical 1970-period POD data

### o INDIVIDUAL MANUFACTURER PROGRAMS

- Interest grew in use of POD concepts for other purposes (1970's)
- Comparison of effectiveness of two penetrants
- Comparison of effectiveness of different NDE techniques

## AEROSPACE INDUSTRY

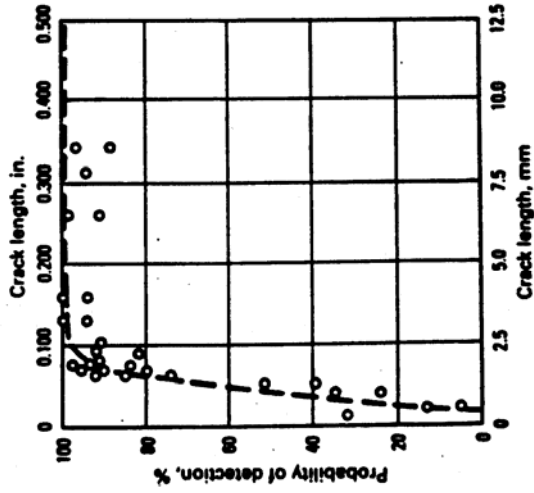
### o EARLY ANALYTICAL METHODS

- Early analyses based on binomial statistics
- Each defect reported as "hit" or "miss"
- Arbitrary averaging used to obtain smoothly increasing curves
- ASNT Standard published in 1982 (now obsolescent)
- POD for single flaw size and confidence level
- Find 29 out of 29 defects to get 90% POD with 95% confidence

### o USAF LED DEVELOPMENT OF NEW STATISTICAL METHODS

- Parametric regression techniques make better use of data
- Incorporated in new MIL-STD for NDE Reliability Assessment (1993?)

**AEROSPACE INDUSTRY**



**Eddy current inspection**



**X-ray inspection**

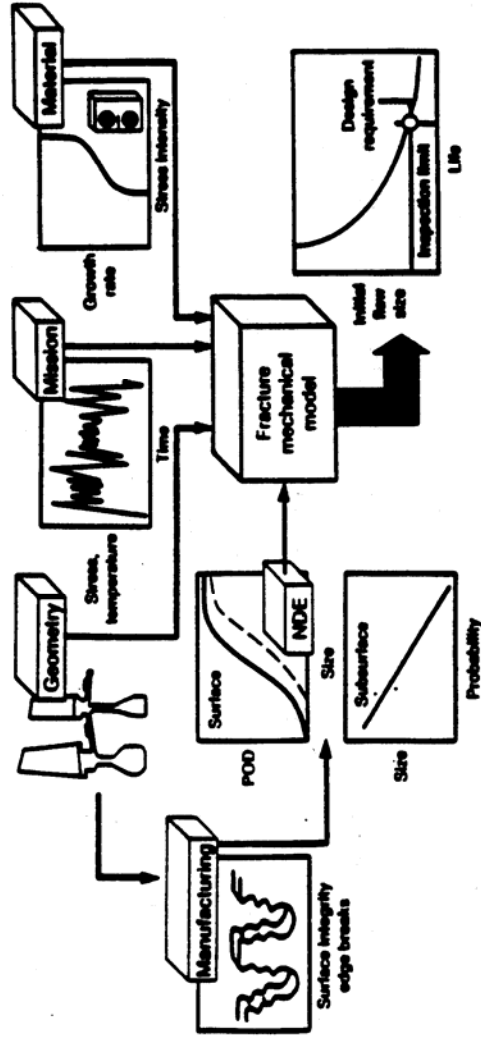
**328 cracks, lengths 0.3 to 18 mm, machined and etched surfaces**

**Typical format for current aerospace POD data**

## **AEROSPACE INDUSTRY**

- o **DESIGN AND LIFING PHILOSOPHIES ARE CHANGING**
  - "Durability" being replaced by "Damage Tolerance"
- o **DAMAGE TOLERANCE**
  - Ability of a structure to resist failure due to flaws or other damage for a specified period of unrepaired usage
  - Invokes fracture-mechanics and POD
  - USAF is encouraging this transition
  - FAA has recommended manufacturers to incorporate damage tolerance concepts (1990 Titanium Review Team Recommendations)

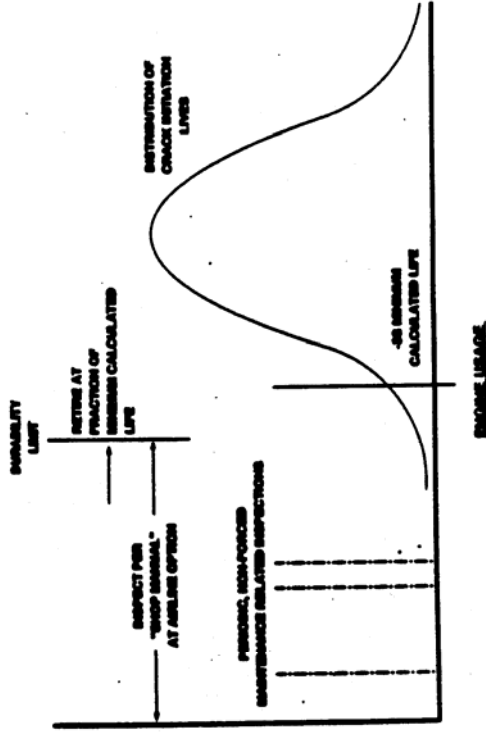
# AEROSPACE INDUSTRY



Outline of a fracture-mechanics model for life-management calculations



## AEROSPACE INDUSTRY



### o **ROLE OF NDE IN DURABILITY DESIGNS**

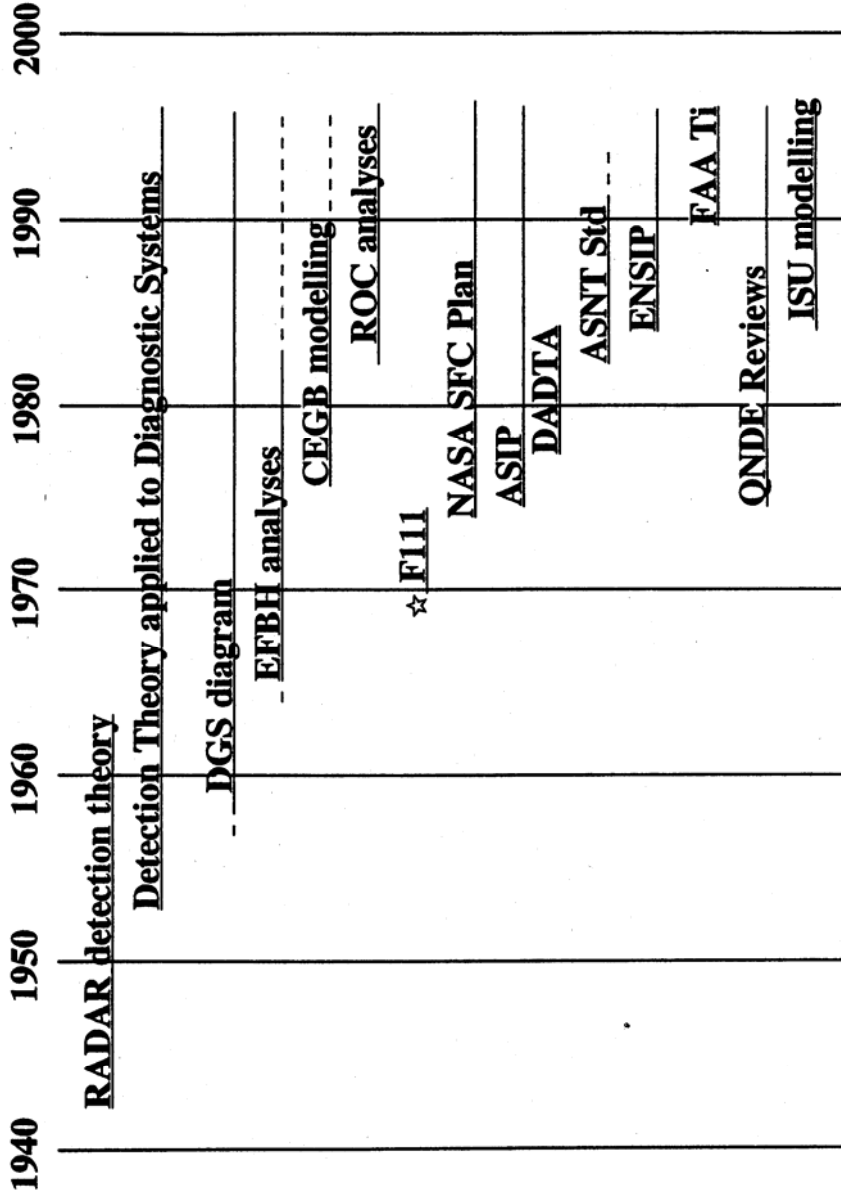
- Design process does not invoke specific capability of NDE processes
- Production parts are assumed to contain no (detectable) defects
- Assumes no in-service damage (resulting in detectable defects) occurs
- NDE is used during manufacture, as a check on process control
- Capability is less important than repeatability and reproducibility
- In-service "inspections of opportunity" are used as added safeguards



## **INTER-INDUSTRY PROGRAMS**

- o **REVIEW OF PROGRESS IN QUANTITATIVE NDE**
  - Started in 1974 under DARPA/AFWAL sponsorship
  - Currently organized by the ISU Center for NDE and Ames Laboratory
  - Cosponsored by ASNT, DOE, FAA, JHU, NIST, NSF, ONR, USAF
  - Numerous publications relating to Reliability, Capability, POD, etc.
  
- o **POD MODELLING (ISU Center for NDE)**
  - Several studies of POD modelling published (since 1985)
    - Mostly for ultrasonic inspection
    - Work in progress on eddy-current and radiography models
  - Recent studies have also included ROC-type analyses

# A PARTIAL CHRONOLOGY



## **SOME ISSUES TO BE ADDRESSED: STANDARDIZATION**

### **o TERMINOLOGY**

- Agreed definitions of specialized terms are needed
- Words like **Capability** and **Reliability** are used loosely & interchangeably
- Need to distinguish defect, process and human effects on detection

### **o PROCEDURES**

- The only existing standard is obsolescent
- The proposed new standard describes current technology, but ...
  - It concentrates on **POD** to the almost total exclusion of **PFA**
  - It is intended for use with simulated defects
  - Problems in relating simulated and natural defects are ignored

### **o GOVERNING ORGANIZATION**

- **ASNT? ... ASTM? ... EPRI? ... FAA? ... ISO? ... NASA? ... USAF?**

## **SOME ISSUES TO BE ADDRESSED: METHODOLOGY**

### **o RANDOM SAMPLING**

- Samples should be selected randomly from our defect population
- We are likely to use all the samples we have available!

### **o POD ALONE OR WITH PFA?**

- POD-versus-size data ignore PFA
- PFA is significant to overall life-cycle cost
- POD-versus-PFA data (usually) ignore defect size
- Defining detectable defect size is crucial in life-management

### **o MEASURE SIGNAL DISTRIBUTIONS OR POD?**

- Basing POD on signal and noise relates NDE to existing detection theory
- Empirical measurements of POD & PFA may be faster and more direct

## **SOME ISSUES TO BE ADDRESSED: MEASUREMENTS**

### **o REAL DEFECTS OR SIMULATED DEFECTS?**

- Measuring POD with simulated defects gives POD for simulated defects
- Need to validate simulated-defect data against natural-defect data

### **o SUBSURFACE INSPECTIONS**

- How do we tell if a natural subsurface defect has been missed?
- An approximate method based only on detected defects has been proposed

### **o CAPABILITY OR RELIABILITY?**

- "Capability" data are often used to represent "Reliability"
- Which is a better description of the inspection process?
  - One set of samples, one inspector, one set of process conditions
  - Various sample sets, inspectors, and process conditions

**SOME ISSUES TO BE ADDRESSED: EXTENDING THE DATA BASE**

**o REDUCE THE COST OF DATA ACQUISITION**

- Detection is affected by numerous factors
- POD must be redetermined if any change is made
  - Slow and expensive
- Need a method to modify existing data bases

**o MODELLING OF INSPECTION PROCESSES**

- Modelling provides a basis for modifying POD data
  - Model defect properties and inspection process parameters
- Models must be evaluated experimentally
  - Data for the modelled defect and the natural defect being modelled



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