

**ELEMENTS OF DETECTION THEORY APPLIED TO NDE**

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## **OUTLINE**

### **o DEFINING "DETECTION"**

- Practical aspects of how we think about detection**
- Differences between detection for specific NDE techniques**
- Effects of automation on detection**
- Effects of imaging on detection**

### **o DETECTION IN A SIGNAL-TO-NOISE CONTEXT**

- A basis for considering detection for all NDE processes?**
- Selected topics in Detection Theory**
- Applying Detection Theory to NDE**

## **DEFINING "DETECTION"**

- o **NDE "DETECTION" IS RARELY DISCUSSED EXPLICITLY**
  - **We probably understand it - but we don't define it**
  
- o **DICTIONARY DEFINITIONS** (Webster's New World Dictionary)
  - **Detect: - to catch or discover, as in a misdeed**
    - **to discover or manage to perceive**  
(something hidden or not easily noticed)
  - **Detection: - a finding out (said especially of what tends to elude notice)**
  
- o **A RADAR DEFINITION** (D.K.Barton, Radar System Analysis)
  - **Target Detection: the process by which the presence of a sought-after object, or target, is sensed in the presence of competing indications which arise from background radiation, undesired echoes, or noise generated in the receiver**

## **DEFINING "DETECTION"**

- o **WE NEED TO DEFINE "DETECTION" BEFORE WE MEASURE "POD"**
  - **Standard NDE handbooks offer little help**
  - **The Radar definition is close to what we need**
  
- o **LET'S REVIEW SOME NDE TECHNIQUES**
  - **Clarify our implicit definition of detection**
  - **Assess whether the Radar definition is suitable for NDE use**

## **INSPECT, TEST, OR EVALUATE?**

- o **DISTINGUISH BETWEEN NDT, NDI, AND NDE?**
  - **NDT, NDI, and NDE are often used interchangeably**
  - **Nondestructive Evaluation can be used as a more comprehensive term**
    - **NDE comprises all NDT and NDI activities**
    - **NDE comprises detection, location, and characterization**
  
- o **DETECTION AND CHARACTERIZATION ARE DISTINCT PROCESSES**
  - **In what follows, POD will refer to detection only**
  - **Caution: this distinction is not always made**
    - **Example: "POD" is sometimes used to express a measurement of performance in detecting and classifying (e.g. sizing) defects**
    - **Better termed "Joint Probability of True Positive" (Joint  $P\{TP\}$ ) or "Probability Of Detection and Correct Interpretation" (PODCI)**

## **DEFECT DETECTION OR DEFECT-FREE MATERIAL?**

### **o SEPARATE BUT RELATED ISSUES**

- **High POD alone does not guarantee defect-free material**

### **o DEFECTS SUCCESSFULLY DETECTED**

- **High POD suffices for selecting NDE techniques**
- **High POD is a necessary but insufficient condition for high product life**

### **o DEFECTS ESCAPING DETECTION**

- **High product life requires a low probability that inspected material still contains any defects (compare Avioli's definition of Reliability)**
- **Requires high POD and low probability of occurrence of defects**
- **High POD may be less important if there is a very low probability of there being a defect in the uninspected material**

## **MAGNETIC PARTICLE AND PENETRANT INSPECTIONS**

- o SENSOR (the eye)**
  - Responds to indication color contrast (dye) or brightness (fluorescent)
  - Responds to indication shape and size (principally length)
  
- o DISCRIMINATOR (the brain)**
  - Records high-contrast and/or large indications - the "signal"
    - Classifies these as "flaws" or "defects" (i.e. above threshold)
  - Ignores low-contrast and/or small indications - the "noise"
    - Classifies these as "irrelevant" or "background" (i.e. below threshold)
  
- o THRESHOLD (set by Specifications, Drawing Notes, etc.)**
  - Typically defines maximum acceptable indication length

## **RADIOGRAPHIC INSPECTION**

- o SENSOR (the eye)**
  - Responds to film contrast and density**
  - Responds to indication shape and size**
  
- o DISCRIMINATOR (the brain)**
  - Records high-contrast and/or large indications - the "signal"**
    - Classifies these as "flaws" or "defects" (i.e. above threshold)**
  - Ignores low-contrast and/or small indications - the "noise"**
    - Classifies these as "irrelevant" or "background" (i.e. below threshold)**
  
- o THRESHOLD (set by Specifications, Drawing Notes, etc.)**
  - Typically defines maximum acceptable indication diameter (or length)**



## **EDDY-CURRENT OR ULTRASONIC A-SCAN INSPECTION**

- o SENSOR (electronic instrumentation)**
  - Responds to indication amplitude
  - Responds to indication depth
  
- o DISCRIMINATOR (an electronic threshold)**
  - Records large indications - the "signal"
    - Classifies these as "flaws" or "defects" (i.e. above threshold)
  - Ignores small indications - the "noise"
    - Classifies these as "irrelevant" or "background" (i.e. below threshold)
  
- o THRESHOLD (set by Specifications, Drawing Notes, etc.)**
  - Typically defines a maximum acceptable indication amplitude
    - Threshold may be related to indication phase (ET) or depth (UT)

## **EFFECTS OF AUTOMATION**

### **o SENSORS**

- **The eye is replaced by electronic or electro-optical devices**
- **Example: machine vision for automated penetrant systems**

### **o DISCRIMINATORS**

- **The brain is replaced by an automatic electronic device**
- **Example: ultrasonic indications signalled by electronic alarm**
- **The discrimination may be more quantitative, and computer-based**
- **Example: penetrant indications may involve measured brightness and size**

### **o THRESHOLDING**

- **Thresholds may be defined more precisely, and may be more complex**
- **Example: "detection" of an indication may be determined by the value of a function of several measured variables**

## **EFFECTS OF IMAGING**

### **o SPATIAL CORRELATION**

- **Imaging presents data from successive interrogations more efficiently**
  - **Takes advantage of spatial correlation of information**
- **Facilitates use of automatic pattern-recognition and decision-making**
  - **Example: a computer can decide if X-ray CT wall-thickness is acceptable**

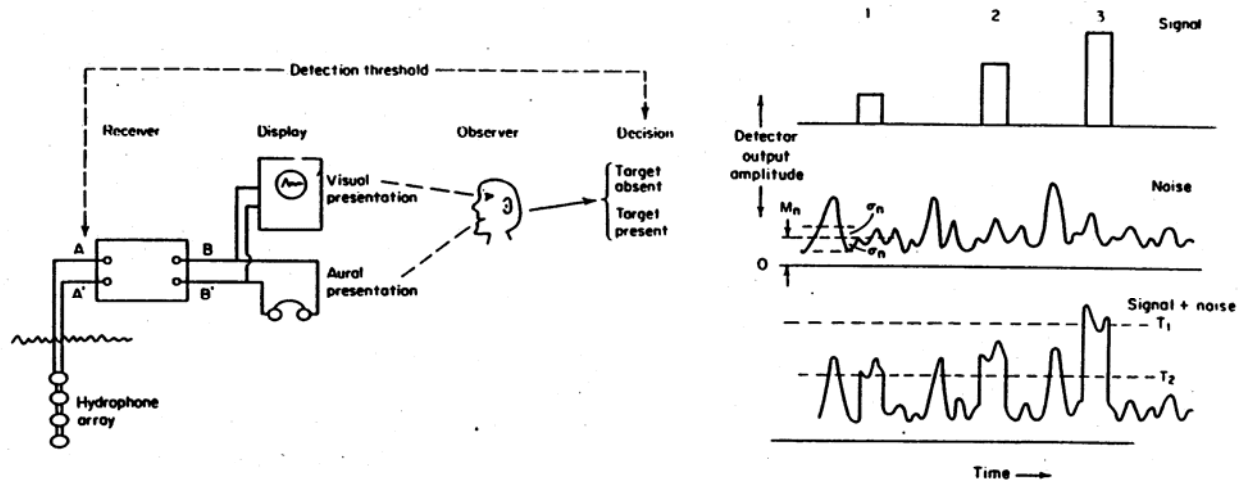
### **o IMAGING DOES NOT CHANGE THE BASIC DETECTION PROCESS**

- **POD is not necessarily improved by imaging**
  - **Example: an A-scan strip-chart contains the same data as a C-scan image**
- **POD may be improved as a result of use a lower discrimination threshold**
  - **In effect, the threshold may be lowered on a local basis**

## **DETECTION AS A SIGNAL-TO-NOISE PROCESS**

- o **NDE TECHNIQUES ARE THRESHOLDED S:N PROCESSES**
  - **Easiest to see this for "electronic" techniques (e.g. ET, UT) and for automated inspection techniques (e.g. computed tomography)**
  - **Basically true for other techniques, too (e.g. MT, PT, RT)**
  
- o **"THRESHOLD"**
  - **Represents a level of discrimination between "signal" and "noise"**
  
- o **"SIGNAL"**
  - **Represents the response from the defects - the sought-after target**
  
- o **"NOISE"**
  - **Competing signals from sources other than defects**

## DETECTION AS A SIGNAL-TO-NOISE PROCESS



**Elements of a receiving system**

**Signals with additive noise**

### **o SONAR DETECTION SYSTEM**

- **Many similarities to ultrasonic NDE**
- **Fundamental concepts are common to most NDE processes**

## **SOURCES OF NOISE**

### **o NOISE FROM THE MATERIAL UNDERGOING INSPECTION**

- **Generic examples:**
  - **Surface roughness**
  - **Edge effects**
- **Process-specific examples:**
  - **Local changes in conductivity (MT, ET)**
  - **Indications from surface pores in castings (PT)**
  - **Grain-boundary reflections (UT)**
  - **Scattering (RT)**

### **o NOISE FROM THE INSPECTION PROCESS ITSELF**

- **Examples:**
  - **Electronic noise (ET, UT)**
  - **Grain structure in film (RT)**

## **VARIATION IN THE DETECTION PROCESS**

### **o DEFECTS**

- **Each defect has slightly different characteristics**
  - **Differences in size, shape, orientation, location, nature**

### **o MATERIAL**

- **Each material sample has slightly different characteristics**
  - **Differences in conductivity, permeability, absorbtivity, etc.**
  - **Differences in shape, surface texture, etc.**

### **o INSPECTION SYSTEM**

- **Each inspection process has slightly different characteristics**
  - **Differences in penetrant concentration, etc.**
  - **Differences in sensitivity, linearity, frequency response, etc.**
- **Each inspector has slightly different capabilities**

## **EFFECTS OF VARIATION**

### **o NUMEROUS PARAMETERS CAN INFLUENCE DETECTION**

- Some have predictable (deterministic) effects
- Many effects are not quantitatively predictable
  - Consequently, detection is a probabilistic phenomenon

### **o IMPERFECTLY CONTROLLED INSPECTION PARAMETERS**

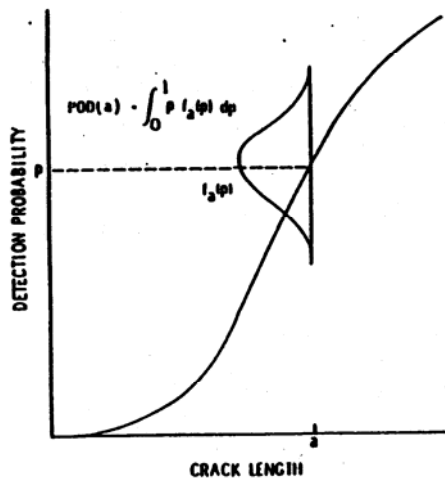
- Perfection is a worthy goal - but always out of reach!

### **o SCATTER IN MEASURED DATA**

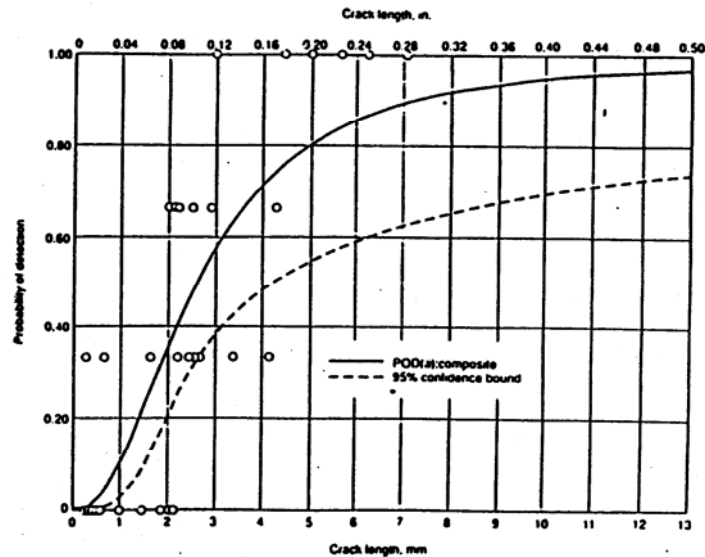
- Both signal and noise data incorporate the effects of variation
  - Measurements will yield distributions of values



## EFFECTS OF SCATTER ON POD



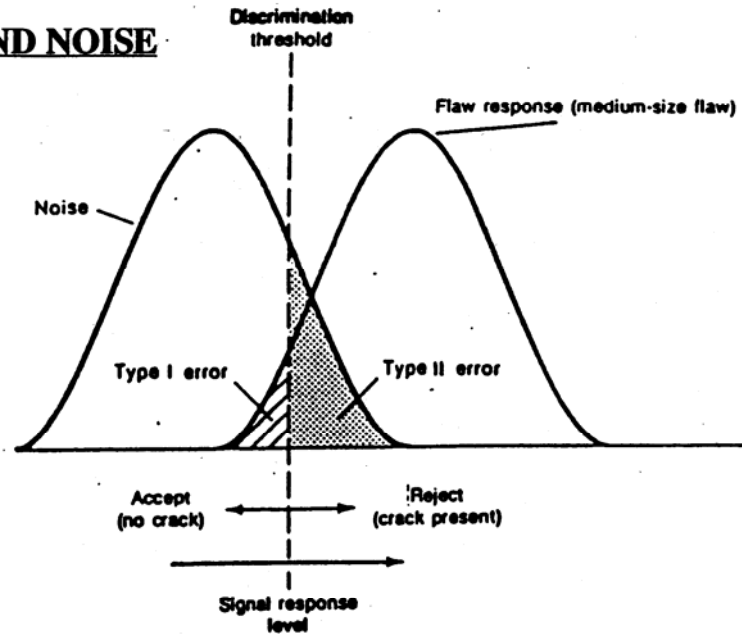
**Probability density function  
of crack detection probabilities  
for cracks of a specific length**



**Probability of Detection data with  
lower one sided confidence bound  
representing the effects of sample  
size and scatter in the data**

## DISTRIBUTIONS OF SIGNAL AND NOISE

A signal-to-noise  
view of detection



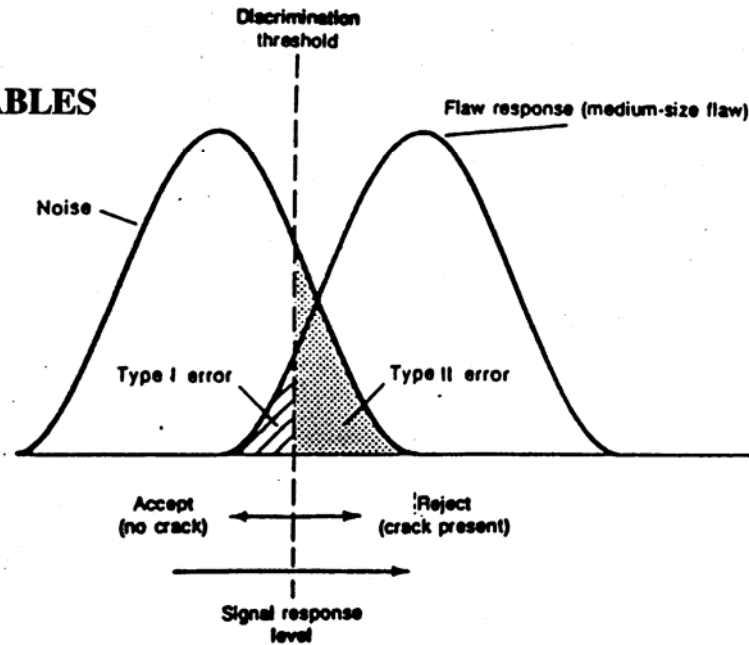
### o AREAS ENCLOSED RELATE TO THE ALTERNATIVE OUTCOMES

- Detection of a defect that is present (POD)
- Non-detection of a defect that is present (1 - POD)
- Apparent detection of a defect that is not present (PFA)
- Non-detection of a defect that is not present (1 - PFA)

## DISTRIBUTIONS OF SIGNAL AND NOISE

### o POD AND PFA ARE CO-VARIABLES

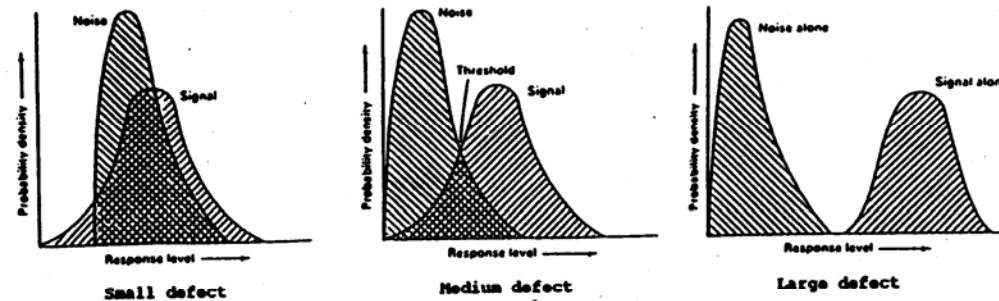
- POD is not a function of PFA
- Both vary with the threshold
- A lower threshold increases POD and PFA



### o CHOICE OF THRESHOLD

- Difficult to keep design and manufacturing engineers happy!
- Reducing Type I errors represents improved product life
- Increasing Type II errors represents increased manufacturing cost

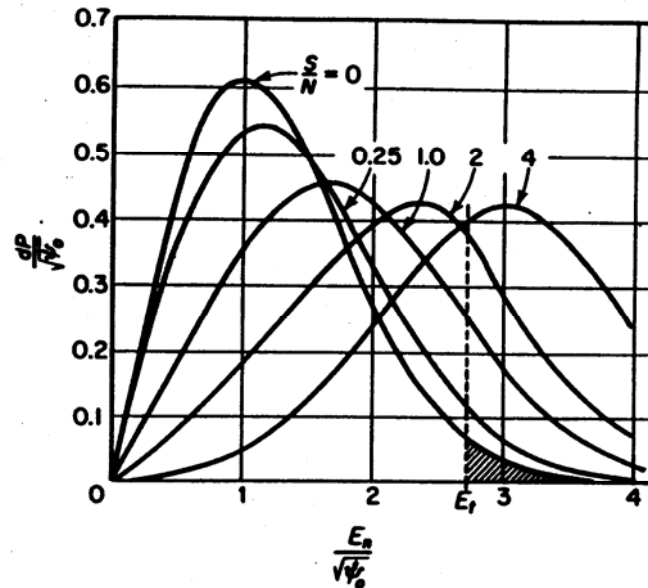
## DISTRIBUTIONS OF SIGNAL AND NOISE



### o DEPENDENCE ON DEFECT SIZE

- Larger defects generally give larger signals
- For a given POD, the PFA will tend to decrease with increasing defect size
- For a given PFA, the POD will tend to increase with increasing defect size
- For a given defect "size", POD also depends on other parameters
  - Shape, orientation, location, nature

## DISTRIBUTIONS OF SIGNAL AND NOISE



### o AN ALTERNATIVE WAY OF LOOKING AT SIGNAL AND NOISE

- Probability distributions of envelope of signal-plus-noise
- Plotted as a function of signal-to-noise ratio (S/N)

## **DISTRIBUTIONS OF SIGNAL AND NOISE**

### **o A GATEWAY TO EXISTING SIGNAL DETECTION THEORY**

- Fifty years of theoretical development and practical application**
- NDE applications have been largely ignored**

### **o STATISTICAL THEORIES OF SIGNAL DETECTION**

- Original applications were to radio communications and radar**
  - Predominantly devoted to analyzing reception of pulsed signals**
- Based on statistical criteria for testing hypotheses and making decisions**
  - Allow derivation of POD and PFA from noise and signal-plus-noise**
  - Allow optimization of receiver/detector design**
  - Provide rationale for choosing a specific detection threshold**

## **DETECTION THEORY**

### **o RESPONSE TO A BINARY STIMULUS**

- **Two possible states of the stimulus**
  - **Noise alone (N)**
  - **Signal plus noise (SN)**
- **Two possible detection decisions (responses)**
  - **Noise alone present**
  - **Signal plus noise present**
- **Four possible outcomes**
  - **N true; choose N ..... true negative ..... probability (1 - PFA)**
  - **N true; choose SN ..... false positive ..... probability PFA**
  - **SN true; choose SN ..... true positive ..... probability POD**
  - **SN true; choose N ..... false negative .... probability (1 - POD)**

### **o THRESHOLDED DETECTION**

- **All observed values greater than the threshold are classed as SN**

## **DETECTION THEORY**

### **o OBSERVED PROBABILITIES**

- Probabilities of decision outcomes are estimated from observed frequencies
- These are conditional probabilities (conditional upon the stimuli)
  - PFA is the probability of an N response given an SN stimulus
  - POD is the probability of an SN response given an SN stimulus

### **o DECISION CRITERIA**

- Rules to help make a choice between the two responses
  - Based on attaching relative importance to the four outcomes
- Of many such criteria, two are of most interest
  - Bayes
  - Neyman-Pearson



## **DETECTION THEORY**

### **o BAYES CRITERION**

- **Assumptions: Observer has information about the source prior to the test**
  - **Prior (or "a priori") probabilities ( $P_1, P_0$ ) are known**
  - **A "cost" ( $C_{10}, C_{00}, C_{01}, C_{11}$ ) can be associated with each outcome**
  - **(These may be truly known or may be educated guesses)**
- **Goal: design the decision criterion to minimize average cost**
- **Problem: it is often difficult to assign prior probabilities and costs**

### **o NEYMAN-PEARSON CRITERION**

- **Assumptions: only the measured conditional probabilities are available**
- **Goal: design a test to minimize PFA and maximize POD**
- **Problem: these are usually conflicting objectives**
- **Solution: set an upper limit to PFA, and maximize POD**

## DETECTION THEORY

### o LIKELIHOOD RATIO TEST

- Bayes and Neyman-Pearson criteria both lead to likelihood ratio tests

- Likelihood Ratio =  $\frac{\text{Probability of choosing SN if SN is true}}{\text{Probability of choosing N if N is true}}$

- The decision depends on whether the likelihood ratio exceeds a threshold

- The threshold used depends on the test

- Bayes test: threshold involves the prior probabilities and costs

$$E_t = [P_0(C_{10} - C_{00})]/[P_1(C_{01} - C_{11})]$$

- Neyman-Pearson test: threshold chosen so that PFA = constrained value

### o AN OPTIMUM RECEIVER

- One that presents at its output the likelihood ratio for each receiver input

- LR =  $\frac{\text{Probability that given amplitude represents SN if SN is true}}{\text{Probability that given amplitude represents N if N is true}}$

## **DETECTION THEORY**

### **o ALTERNATIVE DECISION CRITERIA**

- **"Optimal" performance can be defined in many ways**
  - **Maximize True Positive while restricting False Positive**
  - **Maximize expected value (minimize "costs") of decision**
  - **Maximize percentage of correct decisions**
- **Individual inspectors may apply their own criteria**
  - **Give priority to avoiding false alarms, or to avoiding misses, etc.**

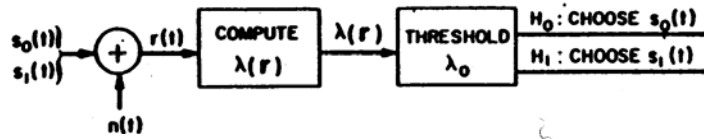
### **o HUMAN FACTORS IN THE DECISION PROCESS**

- **Inadequately trained inspectors use widely varying decision criteria**
  - **Human criteria tend to change with experience and/or training**
    - **e.g. both POD and PFA tend to decrease with time if SN is small**

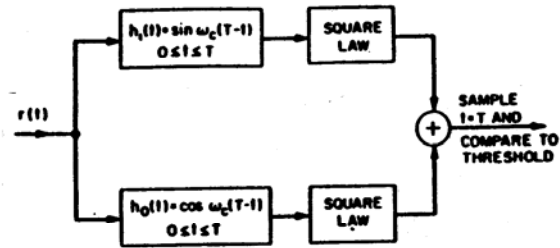
### **o AUTOMATED INSPECTION**

- **Decision criteria may vary, but are applied consistently**

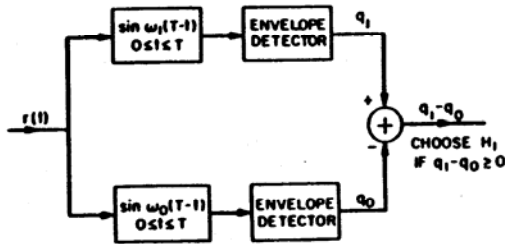
# DETECTION THEORY



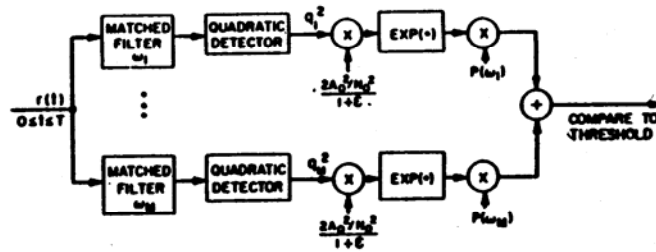
Binary communication signals



Signals of random phase



Signals of random amplitude and phase



Rayleigh fading signals of unknown frequency

## o EXAMPLES OF OPTIMUM RECEIVERS

- Signals with known or random parameters
- Signals corrupted by additive white Gaussian noise

## **DETECTION THEORY**

- o MEASUREMENT OF CONDITIONAL PROBABILITIES**
  - Produce the stimulus and measure the response**
  - Base estimates of probabilities of outcomes on observed frequencies**
  
- o COMMUNICATIONS, RADAR, SONAR: relatively easy to accomplish**
  - Switch on the signal source(s), or tell the pilot where to fly**
  
- o NONDESTRUCTIVE EVALUATION: much more of a challenge**
  - Stimuli are much more varied**
  - True stimuli are natural, not manufactured**
  - A "referee" technique is needed to identify the SN stimulus**
    - For surface defects this might be optical microscopy**
    - For subsurface defects no such technique exists**

## **DETECTION THEORY**

### **o USE OF NATURAL DEFECTS**

- **Most desirable way of sampling the real defect population**
  - **May be difficult to obtain a truly representative sample**
  - **Good material quality means that defects are rare**
- **Adequate characterization may present difficulties**
  - **Destructive examination is costly - and destroys the sample!**

### **o USE OF ARTIFICIAL DEFECTS**

- **Allows control of at least some of the defect characteristics**
  - **Size, shape, orientation, location, nature**
- **Difficult to truly represent the real defect population**
  - **What we measure is the POD for the artificial defect type**
  - **Still need to validate these measurements against natural defects**

## **DETECTION THEORY**

### **o SELECTION OF MEASUREMENT CONDITIONS**

- **Goal of measurement must be clearly defined**
  - **Determines the inspection parameters**
- **Measure "Capability"**
  - **One inspection of a sample of defects of "identical" or differing size**
- **Measure "Repeatability"**
  - **Multiple measurements of a defect sample by the same inspector/system**
- **Measure "Reproducibility"**
  - **Multiple measurements of a defect sample using "identical" conditions**
- **Measure "Variability"**
  - **Multiple measurements of a defect sample by different inspectors/systems**
- **Measure "Reliability"**
  - **Multiple measurements of a defect sample using all these factors**

## **DETECTION THEORY**

### **o MEASUREMENT OF POD ALONE**

- **Acceptable: POD is not dependent on PFA**
  - **Knowledge of POD is adequate for determining capability and reliability**
  - **Knowledge of POD is adequate for predicting product life**

### **o MEASUREMENT OF POD AND PFA**

- **Recommended: a more complete description of the detection process**
  - **Knowledge of PFA helps select an optimum threshold**
  - **Knowledge of PFA helps identify manufacturing costs**

### **o MEASUREMENT OF ALL FOUR OUTCOMES**

- **Not recommended: POD and PFA fully describe the detection process**
  - **Probability of a false negative (a miss) is the complement of POD**
  - **Probability of a true negative is the complement of PFA**



## **SOURCES USED**

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